



Modeling the Effects of Spacecraft Venting on Instrument Measurements of the Martian Atmosphere for an Elliptical Orbit

Elaine Petro (NASA/GSFC)

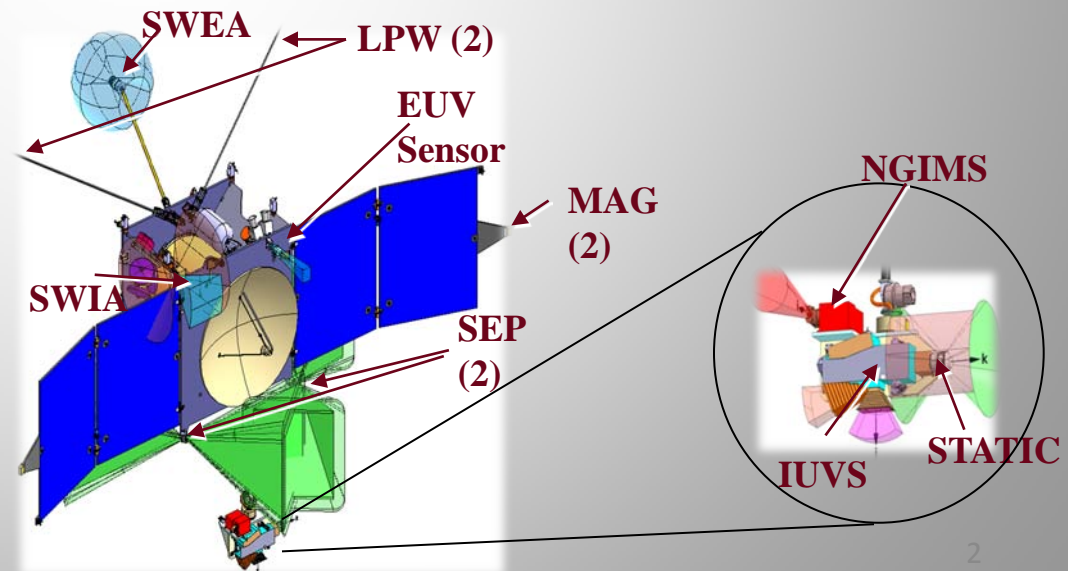
David Hughes (NASA/GSFC)

Contamination, Coatings & Materials Workshop
July 12-14, 2011



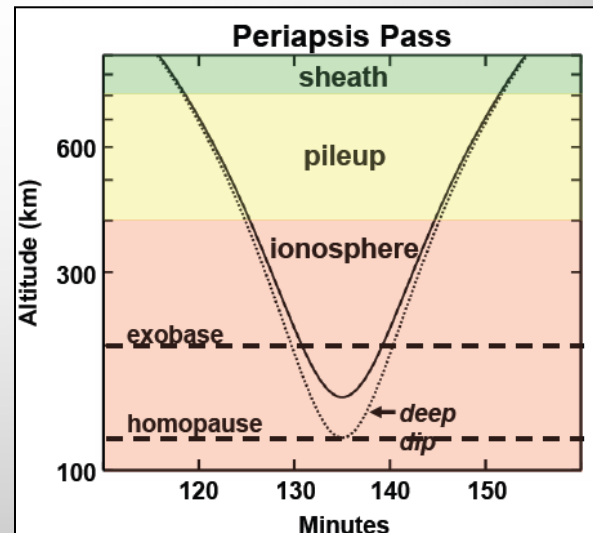
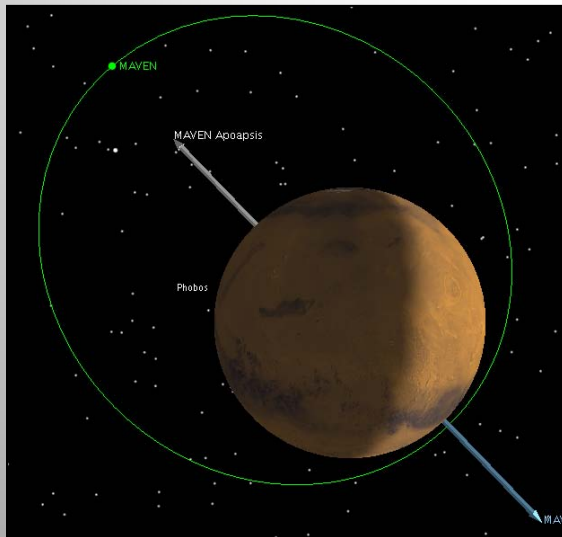
Background

- Analysis performed for MAVEN mission
 - Will study the Martian atmosphere, ionosphere, and interactions with sun and solar wind
 - Emphasis on the loss of volatile compounds (CO_2 , NO_2 , H_2O) from the atmosphere to space



Background

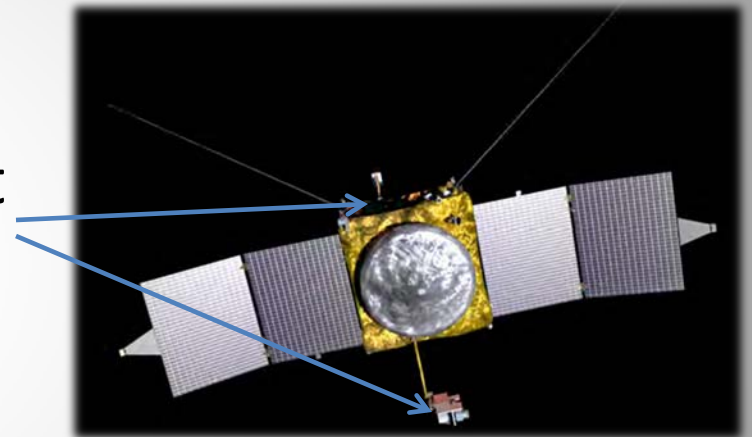
- Elliptical science orbits:
 - Nominal: 150 km x 6220 km altitude with 4.5 hour period
 - ‘Deep Dip’: Periapsis altitude lowered to 125 km to measure higher density regions
- Large pressure range (10^{12} Pa at apoapsis, 10^6 Pa at nominal periapsis, 10^5 Pa at Deep Dip periapsis)





Background

- With large pressure variations in orbit, need to understand how internal pressures change
- Internal pressures may track but also lag atmospheric pressure
- Flux of gas from vents could potentially bias instrument measurements



Goal: Predict the effect that atmospheric gases trapped and vented from spacecraft volumes could have on instrument measurements.



Approach

- **Ambient Atmosphere**
 - Determine properties throughout orbit
 - Analyze pressures on surfaces accounting for s/c orientation and velocity
- **Flow Across Vents**
 - Calculate molecular flow vent properties of all major volumes (instruments, spacecraft)
 - Perform transient flow across vents to predict pressures inside volumes
- **Free Molecule**
 - Predict redistribution of gases from vents with molecular transport analysis

Ambient Atmosphere

1. Orbit Prediction
2. Mars Atmosphere
3. Effective Pressures

Vent Flow

1. Vent Conductance
2. Mass Conservation ODE
3. FM Source Fluxes

Free Molecule Transport

1. Direct Flux
2. Reflected Flux

Fluxes of
ambient gases

Flow across
vents

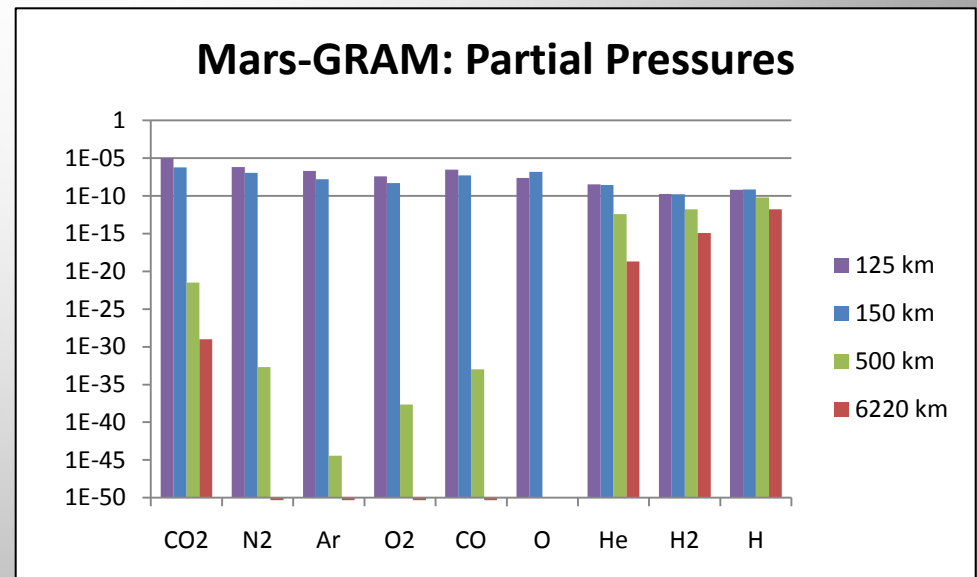
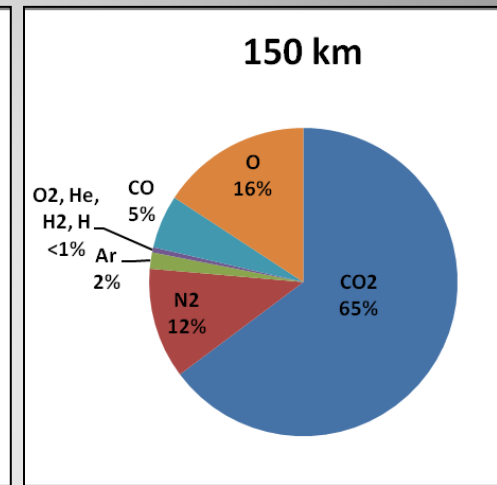
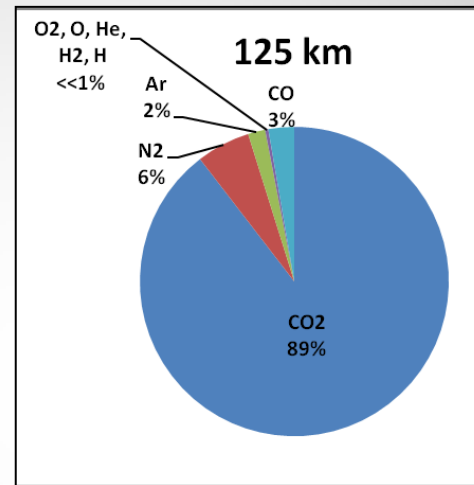
Fluxes of
vented gases



Ambient Steps 1 & 2



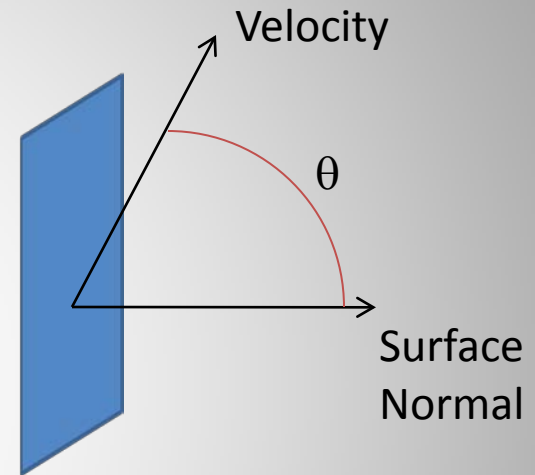
- Orbit position prediction
 - Calculated using Keplerian orbital elements
 - $a = 6578 \text{ km}$
 - $e = 0.462$
 - $i = 75^\circ$
 - No perturbations
- Mars atmosphere
 - Mars Global Reference Atmospheric Model 2005 (Mars-GRAM)
 - Maintained by Marshall Space Flight Center
 - Used to calculate density and composition of ambient species





Ambient Step 3

- Effective pressures calculated for each element
 - Function of:
 - ambient density (ρ)
 - spacecraft velocity (v)
 - average molecule velocity (u)
 - element surface to flow angle (θ)
 - Incorporated new ‘ram impingement’ mass flux model¹:
 - Velocity scale factor (s)
 - Mass flux calculated using scale factor



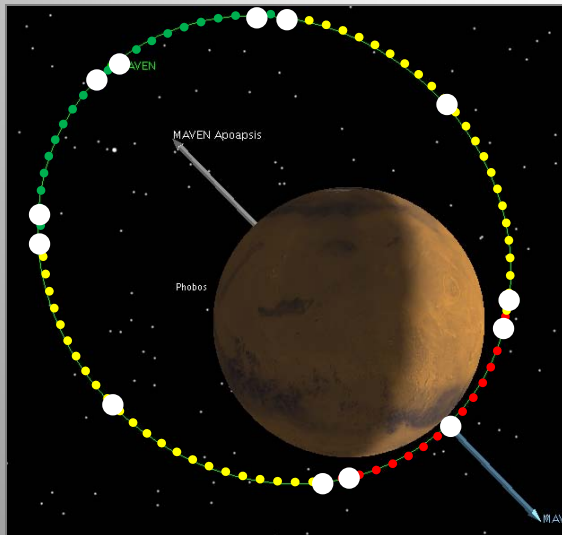
$$s = -\frac{v}{u} \cos \theta$$
$$\dot{m} = \rho u \sqrt{\frac{1}{4\pi}} \left(e^{-s^2} + \sqrt{\pi} [1 + \operatorname{erf}(s)] \right)$$

¹J. Borde, P. Renard, G. Sabbathier, G. Drolshagen, “Improved Analysis Tool for the Computation of Spacecraft Surface Erosion Due to Atomic Oxygen,” *Proceedings of the Sixth International Symposium on Materials in a Space Environment*, **271**, ESTEC, Noordwijk, The Netherlands, 19-23 September 1994.



Effective Pressure Calculations

- ‘Effective pressures’ calculated for 13 discrete points in orbit
 - Atmospheric density and spacecraft orientation vary
 - Sum of direct flux of impinging atmospheric molecules and reflected flux off spacecraft surfaces

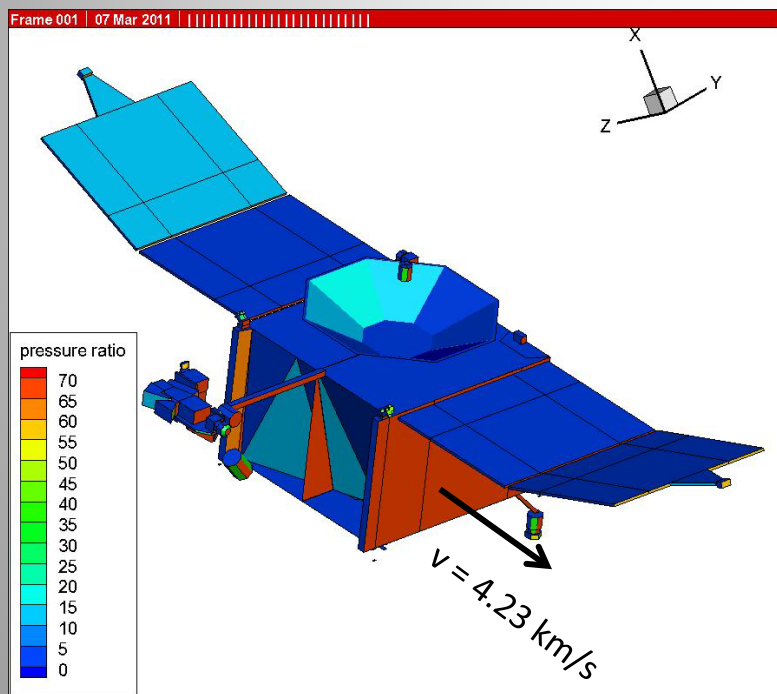


| Orbit Segment | Possible Orientations |
|--|----------------------------------|
| Below 500 km (Deep Dips) | “Fly – Z” |
| Below 500 km (nominal) | “Fly – Y” Sun Velocity |
| 500 km – 5200 km (sides) | Sun Nadir Sun Inertial |
| Above 5200 km (apoapse region) | Sun Inertial |

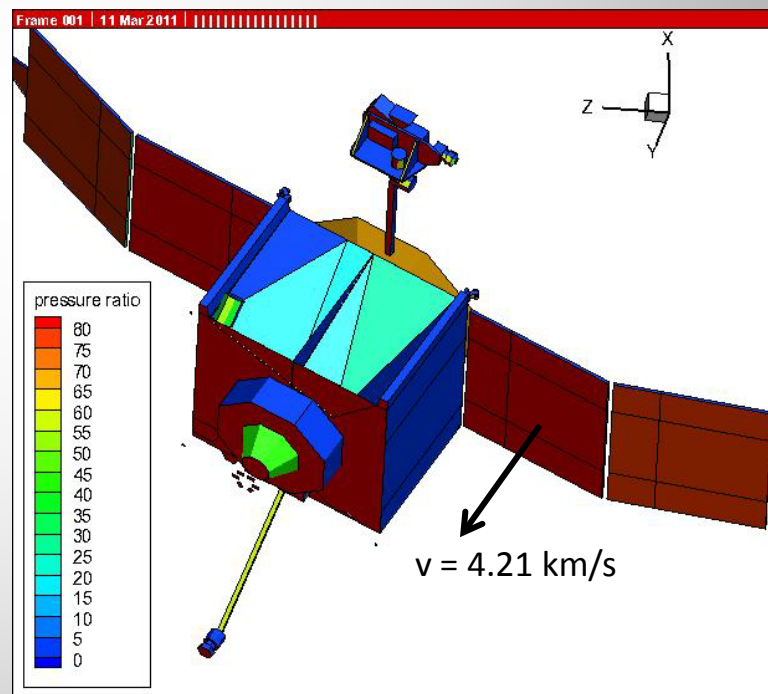


Effective Pressure Results

- Ratio of effective pressure to ambient pressure shown below for periapsis of nominal orbit (left) and Deep Dip (right)
 - Max effective pressures about 70x ambient (150 km) and 80x ambient (125 km)



Effective Pressure / Ambient Pressure
(150 km)



Effective Pressure / Ambient Pressure
(125 km)



Flow Calculations (Step 1)



- Depressurization time constant (τ) used to compare efficiency of different vents:
 - Time for ΔP to drop by factor of e
 - Function of inner volume (V) and vent conductance (C)
- Conductance (C) is a measure of the ease at which gases flow through a duct
 - Analytical solutions available for simple vents
 - Complex geometries require numerical solution

Time constant:

$$\tau[s] = \frac{V[m^3]}{C[m^3 / s]}$$

Circular tube of constant cross section:



$$C = \frac{2\pi R^3 v}{3L} \cdot K''$$

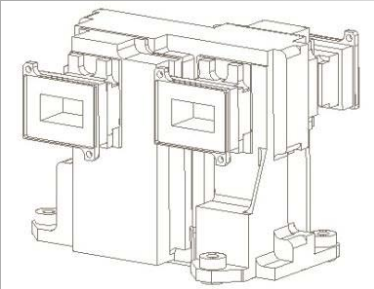
Multiple vents in parallel:

$$C_{eq} = C_1 + C_2 + \dots + C_N$$

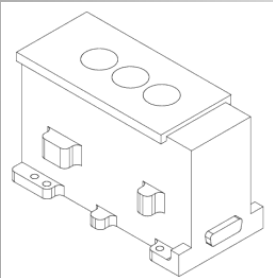


Sample Vent Geometries

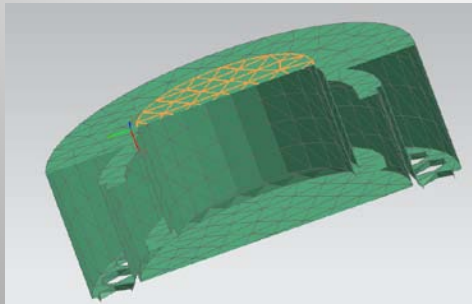
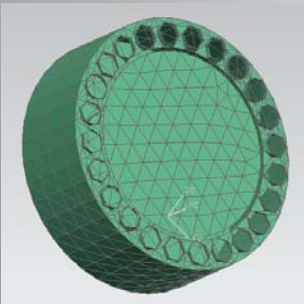
- Various instrument



4 identical baffles
*(tapered rectangular
tubes in parallel)*



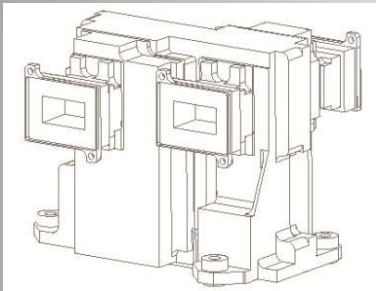
3 aperture holes
*(short circular tubes in
parallel)*



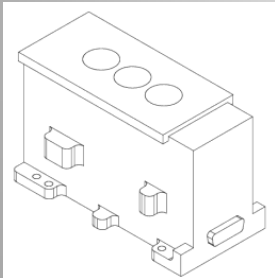
Labyrinth vent
(GBVF analysis)

Sample Vent Geometries

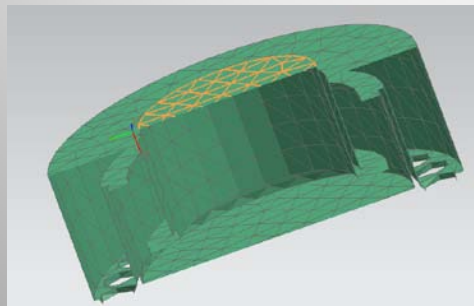
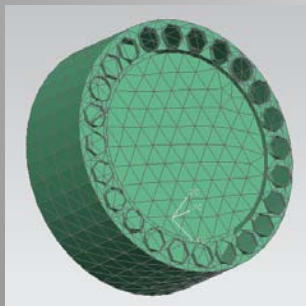
- Various instrument vents:



4 identical baffles
(tapered rectangular tubes in parallel)



3 aperture holes
(short circular tubes in parallel)



Labyrinth vent
(GBVF analysis)

- Labyrinth vent required gray body viewfactor (GBVF) analysis

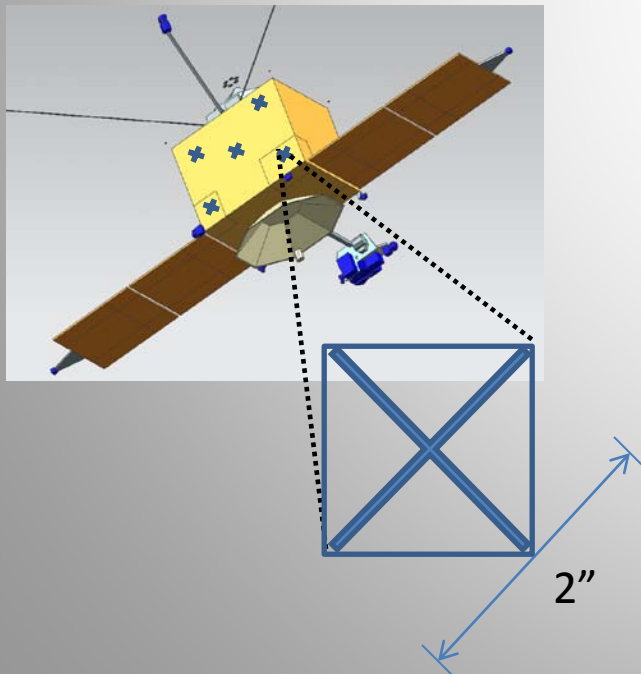
- Set the entrance and exit sticking coefficient to 1, all others to zero
- GBVF solved using Gebhart's method (matrix inversion)
- GBVF from entrance to exit is the transmission probability (k)
- Conductance of a tube is aperture conductance times transmission probability:

$$C = \left(\frac{1}{4} vA \right) (k)$$



Vent Comparison

- Time constants (volume/conductance) compared for 11 instrument vents and spacecraft bus vents
 - Spacecraft bus venting found to be limiting case
 - S/C provider using 2x2" x-cuts in MLI to vent bus interior (24 cuts assumed)
 - Assumed cut width of 1/16", MLI thickness of 1/4"

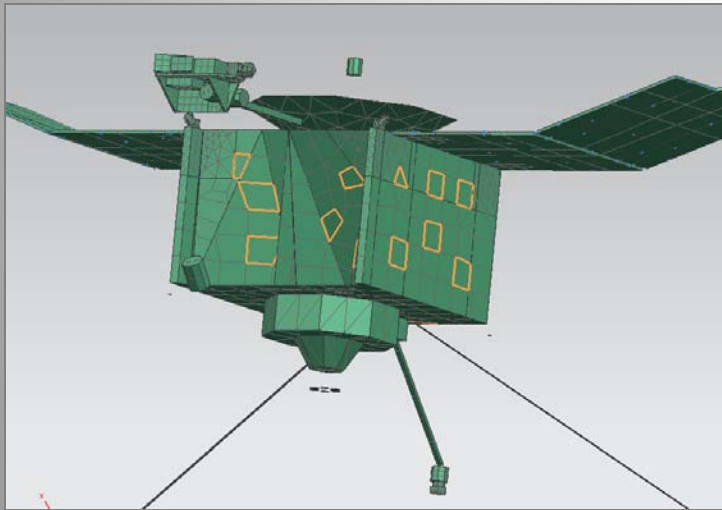


| Component | Open Volume (m ³) | Conductance (m ³ /s) | Time Constant (s) |
|------------------------------|-------------------------------|---------------------------------|-------------------|
| <i>Spacecraft Bus Vents</i> | | | |
| Spacecraft Bus ¹ | 4.46 | 0.15 | 29 |
| <i>Instrument Vents</i> | | | |
| IUVS | 8.35e-2 | 0.023 | 0.4 |
| NGIMS | 4.36e-3 | 0.003 | 3.0 |
| RSDPU | 5.41e-3 | 0.00076 | 2.0 |
| SWIA/SWEA/STATIC Aperture | 1.34e-4 | 1.8e-5 | 7.4 |
| SWIA/SWEA/STATIC Electronics | 1.9e-3 | 0.0012 | 1.6 |
| SEP ³ | 4.16e-4 | 0.042 | 0.01 |
| MAG | 3.69e-4 | 0.0017 | 0.21 |
| EUV | 7.67e-4 | 0.73 | 0.01 |
| LPW (Pre-amps) | 1.74e-5 | 0.0004 | 0.04 |
| LPW (Stacers) | 1.74e-4 | 0.11 | 0.002 |

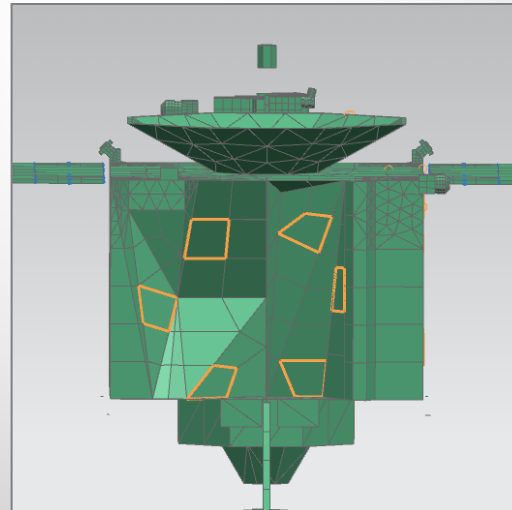


FEM and Vent Placement

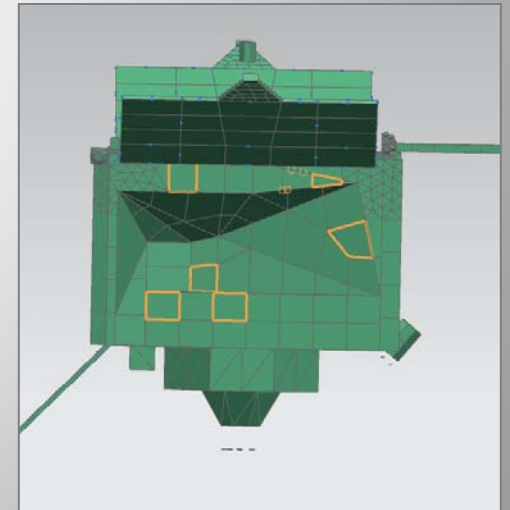
- 24 vents were divided evenly between 4 lateral faces (+X, -X, +Y, -Y)
- Elements selected to represent vent locations (spread out across face)



+X and +Y vent locations



-X vent locations



-Y vent locations



Flow Calculations (Step 2)



- Solved for pressure inside spacecraft bus at each time step
 - Transient ambient pressures on the vent FEM elements used as boundary conditions to solve gas flow differential equation:

$$V \frac{dP}{dt} = C(\Delta P)$$

- Solved separately for each species
 - Travel independently of one another in molecular flow regime
- Solved in log scale of pressure to avoid negative numbers (pressure boundary condition had dynamic range of 1e-5 to 1e-70)

$$\frac{d(\ln P)}{dt} = \frac{1}{P} \frac{dP}{dt}$$

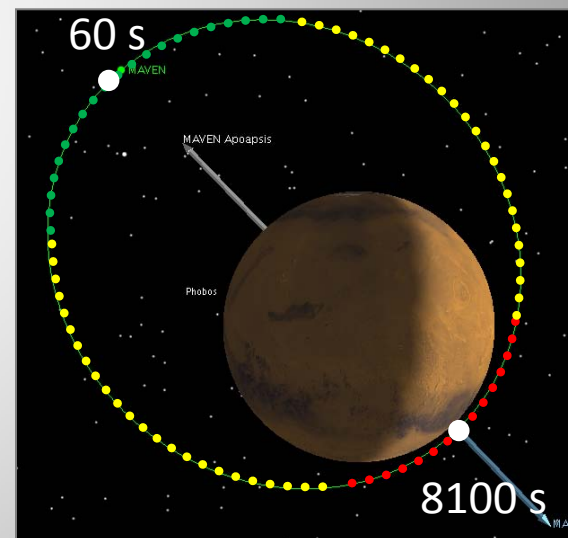


Step 2 Results

- Tracking each species independently gave composition of gas interior and exterior to bus

| Time since Apoapsis (sec) | Altitude (km) | Internal Bus Pressure (Pa) | Atmospheric Pressure (Pa) | Bus/Amb % Comp Ratio CO ₂ | Bus/Amb % Comp Ratio He | Bus/Amb % Comp Ratio H |
|---------------------------|---------------|----------------------------|---------------------------|--------------------------------------|-------------------------|------------------------|
| 60 | 6220 | 1.5e-11 | 1.7e-12 | 1.00 | 1.00 | 1.00 |
| 1350 | 6025 | 9.2e-12 | 1.4e-12 | 0.94 | 1.00 | 1.00 |
| 1575 | 5950 | 1.0e-11 | 1.6e-12 | 0.97 | 0.998 | 1.00 |
| 4050 | 4425 | 3.1e-11 | 4.4e-12 | 0.96 | 0.91 | 1.00 |
| 6750 | 1250 | 7.1e-10 | 4.0e-11 | 0.59 | 0.98 | 1.00 |
| 7425 | 475 | 2.2e-09 | 1.9e-10 | 0.99 | 1.00 | 1.00 |
| 8100 | 150 | 2.1e-05 | 9.8e-07 | 1.00 | 0.96 | 0.96 |
| 8775 | 475 | 5.8e-09 | 2.3e-10 | 1.06 | 1.00 | 0.999 |
| 9450 | 1250 | 3.1e-09 | 1.9e-10 | 0.58 | 0.90 | 1.02 |
| 11925 | 4215 | 3.5e-11 | 4.4e-12 | 1.00 | 0.97 | 1.00 |
| 14625 | 5950 | 1.4e-11 | 2.1e-12 | 0.98 | 0.999 | 1.00 |
| 14850 | 6025 | 8.1e-12 | 1.7e-12 | 0.96 | 1.00 | 1.00 |
| 16200 | 6220 | 1.0e-11 | 1.3e-12 | 1.00 | 1.00 | 1.00 |

$$Ratio(species) = \frac{\left(\frac{Partial\ Pressure(species)}{Total\ Pressure} \right)_{bus}}{\left(\frac{Partial\ Pressure(species)}{Total\ Pressure} \right)_{ambient}}$$



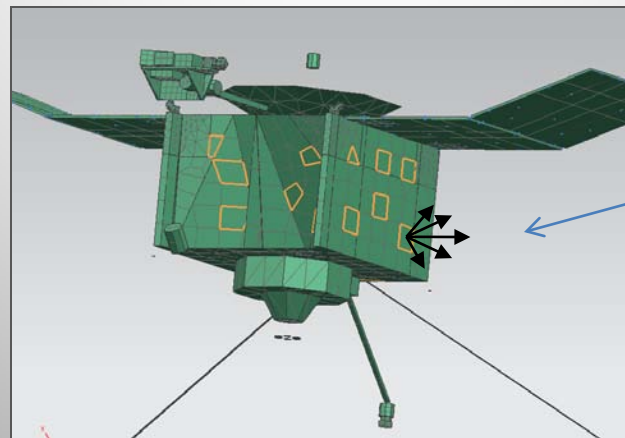
Largest composition deviation, but how much of this gas actually makes it to the instrument apertures?



Flow Calculations (Step 3)



- Determine Free Molecule source terms
 - Used pressure inside spacecraft to determine flux through the vents to the outside
 - Did not use external pressure: inward flow is independent of outward flow in the free molecule regime
 - Converted to mass flux and treat as effusion source (Lambertian distribution, thermal velocity)



Effusion source

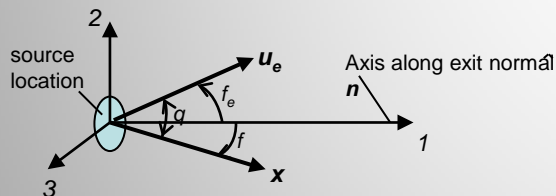


Free Molecule Calculations



- Direct Flux

- Use solution of Boltzman equation to calculate gas flux to surfaces with a line of sight to the vents
- M. Woronowicz, *Rarefied Gas Dynamics: 22nd International Symposium*, AIP, **585**, Melville, NY, 2001, pp. 798-805



$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \frac{\partial f}{\partial \mathbf{x}} = Q_1;$$

$$Q_1 = \frac{2\beta^4}{A_1 \pi} \delta(\mathbf{x}) \dot{m}(t) (\mathbf{v} \cdot \hat{\mathbf{n}}) \exp(-\beta^2 (\mathbf{v} - \mathbf{u}_e)^2);$$

$$A_1 \equiv e^{-s^2 \cos^2 \phi_e} + \sqrt{\pi} s \cos \phi_e (1 + \operatorname{erf}(s \cos \phi_e)).$$

- Reflected Flux

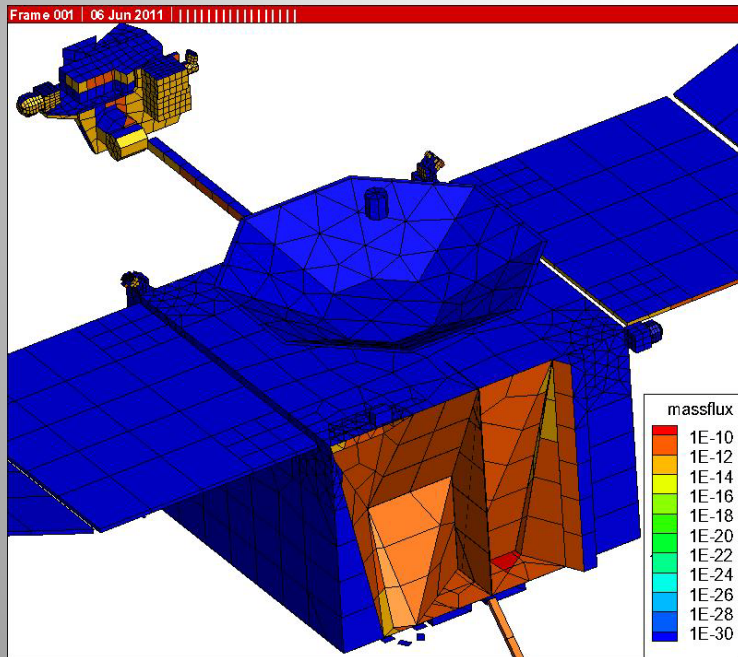
- Assume that all of the flux reaching a surface is reflected
- Treat as a new effusion source
- Add contributions to FEM elements to approximate the molecular transport solution

- Limitation of method

- Does not account collisions between reflected and incoming molecules
 - Possible reduction in what reaches the surface
- Did not repeat iteration to extend “view” to surfaces requiring more than one bounce to reach

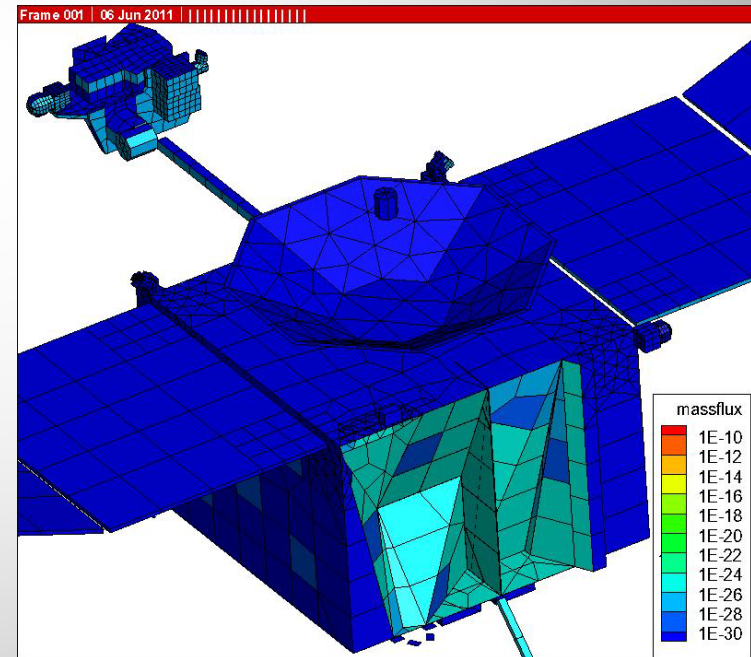
Free Molecule Results

- Direct Flux
 - Max value is 10^{-10}



CO₂ @ 125 km - Direct

- Reflected Flux
 - Max value is 10^{-25}



CO₂ @ 125 km – One Reflection

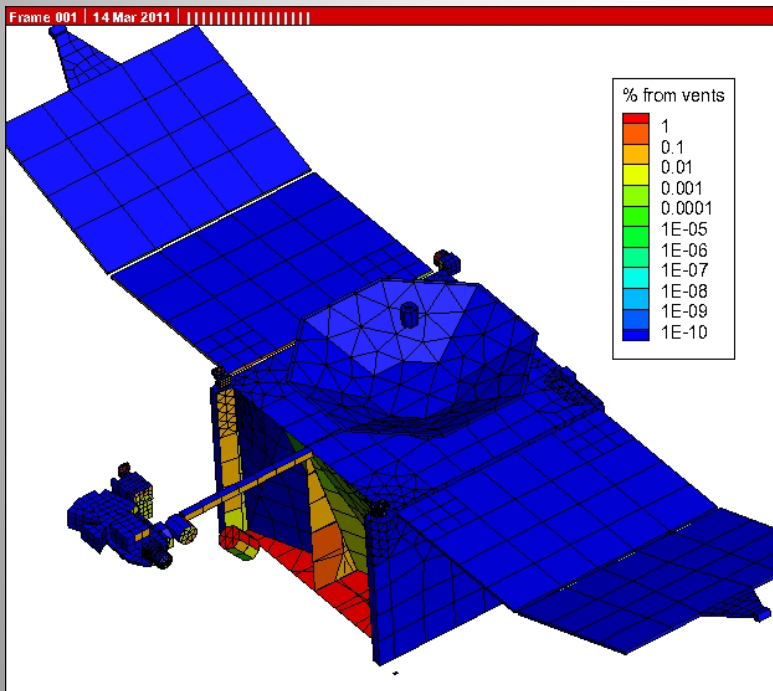


Analysis of Results – Deep Dip Orbit

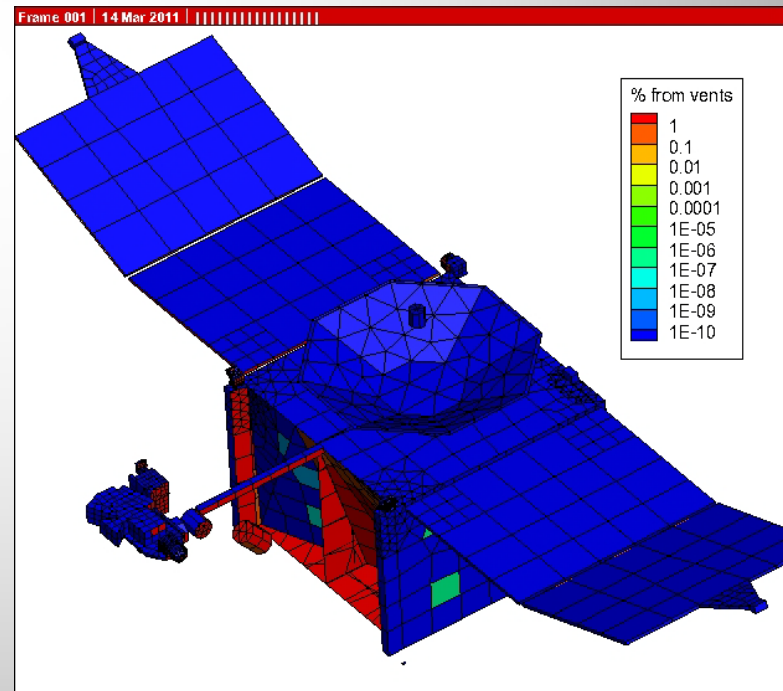


- Spacecraft colored by percent of impinging flux originating from vented gas
 - Project interested in amount **relative** to atmospheric flux

$$\% = \frac{\Phi_{\text{vent,in}}}{\Phi_{\text{vent,in}} + \Phi_{\text{amb,in}}} \times 100\%$$



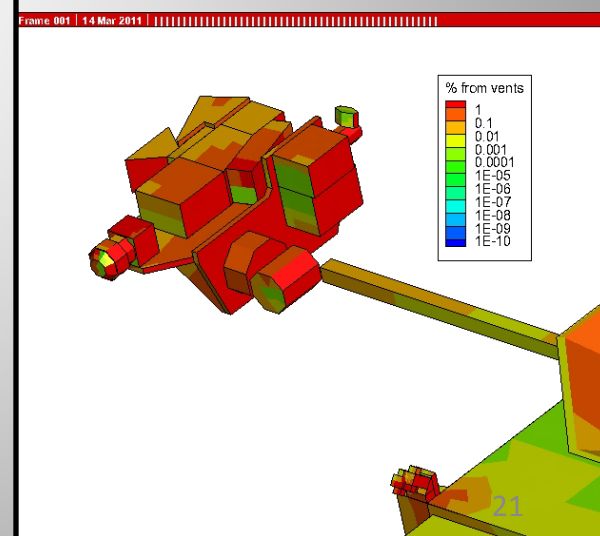
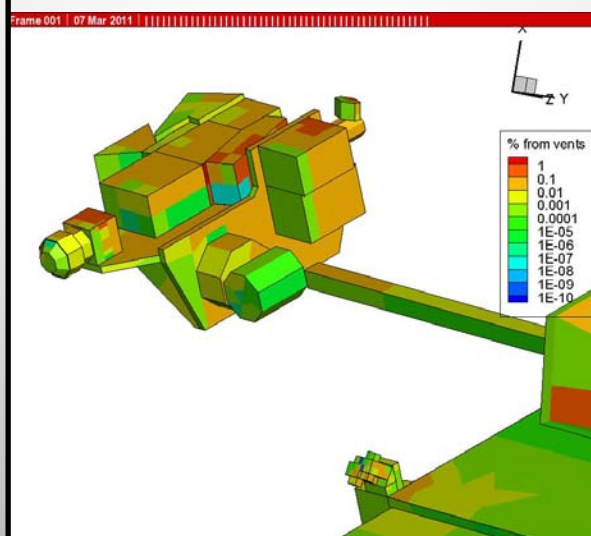
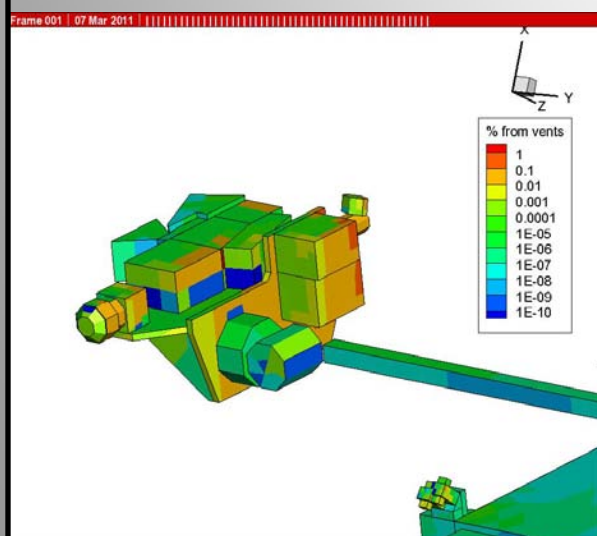
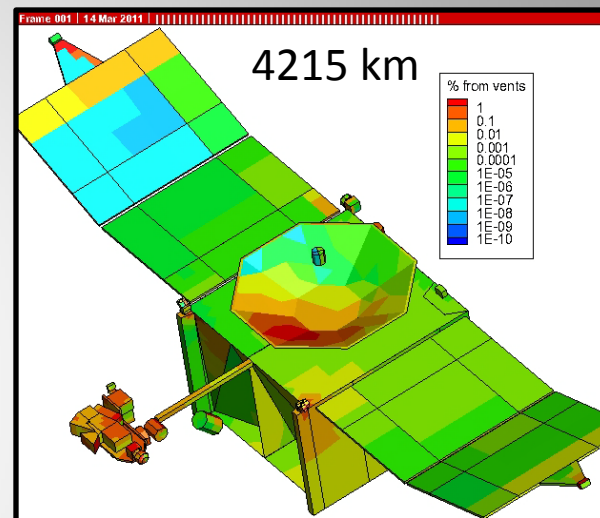
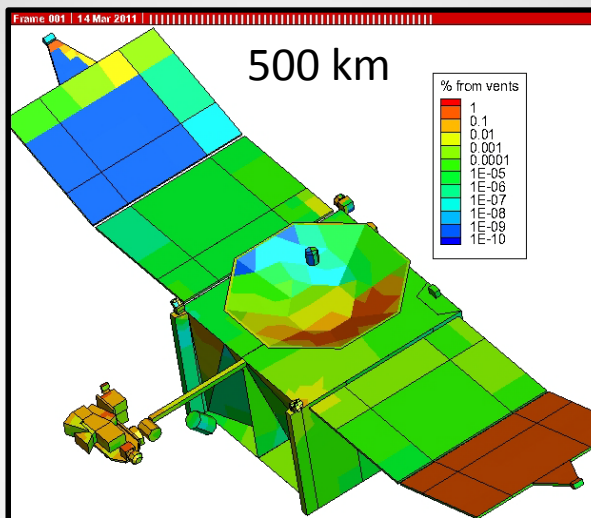
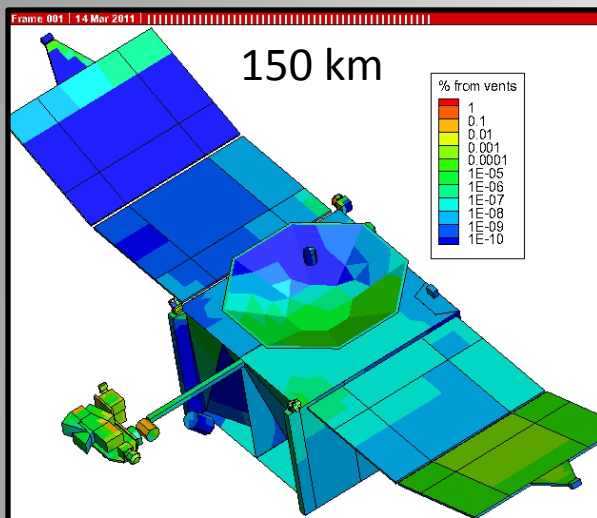
125 km (periapsis)



500 km (traveling out)



Analysis of Results – Nominal Orbit





Conclusions

- Analysis required unique implementation of direct/reflect flux and pressure calculation methods
 - Able to prove that vented gas does **not** pose a serious threat to instrument measurements for MAVEN
- For similar analysis in future:
 - Would implement spacecraft slew in Nx calculations (more automated)
 - Would incorporate shadowing from other surfaces in ram pressure calculations



Thank you!